

Sylhet Cadet College
Pre-Test Examination - 2022
Class: XII
Set - B

Subject: Statistics 2nd Paper (Creative)

Time: 2 hour & 35 minutes

Subject Code: 130

Full Marks: 50

Answer FIVE questions taking at least two (2) from each group. Figures in the right indicate full marks.

Group A

1. **Sadman has an urn with 5 red and 4 white balls. He has randomly drawn two balls from the urn.**

- (a) What is the probability of an uncertain event? 1
- (b) Write the third axiom of probability. 2
- (c) What is the probability that both the balls drawn by Sadman are white? 3
- (d) Are the probabilities of both balls being same color and different color equal? Analyze. 4

2. $P(A) = \frac{3}{10}, P(B) = \frac{2}{5}, P(B \cup A) = \frac{1}{2}$

- (a) What is an independent event? 1
- (b) What is the relationship between independency and mutual exclusivity? 2
- (c) Find $P(A|B)$ and $P(B|A)$ 3
- (d) Verify the equality mathematically & empirically: $P(B) = P(A) \cdot P(B|A) + P(\bar{A}) \cdot P(B|\bar{A})$ 4

3. **The probability density function of a continuous random variable is**

$$f(x) = kx^2 + kx + \frac{1}{8}; 0 \leq x \leq 2$$

- (a) What is a continuous random variable? 1
- (b) Find the value of k 2
- (c) Find the probability that the values of x would lie between 1 and 3. 3
- (d) Find $P(1 \leq X \leq 3)$ 4

4. **The joint probability function of two random variables X & Y is given below:**

$$P(x, y) = \frac{1}{21}(x + y); x = 1, 2, 3 \text{ \& } y = 1, 2$$

- (a) What is a probability density function (pdf)? 1
- (b) What is $P(X=a)$ in a pdf, where a is an arbitrary number? 2
- (c) Find the marginal probabilities. 3
- (d) Find $P(x|y), P(x|1)$ and $P(y|4)$ 4

Group B

5. **Sakib has recently graduated from the University of Dhaka. he applies to two firms - EduCube & Digidig- for a Data Analyst job. The probability of hiring by EduCube is 0.8 and by Digidig is 0.4. The probability that none hires is 0.5.**

- (a) What is a sample space? 1
- (b) Explain how to find $P(\bar{A} \cap B)$ using Venn Diagram. 2
- (c) Find the probability of hiring by Digidig but not by EduCube. 3
- (d) Find the probability that no firm will reject him. 4

6. **Two dice are thrown together. The dice are named A and B.**

- (a) What is $P(A=7)$? 1
- (b) Create the sample space. 2

- (c) What is the probability that the outcomes of A & B are different? 3
- (d) Determine the probability that the summation of outcome of two dice is a prime number. 4

7. **A magician draws two cards from a pack (i) with replacement and then (ii) without replacement. The cards were well-shuffled before drawing.**

- (a) What is the probability of an impossible event? 1
- (b) How to determine the probability of a joint event? 2
- (c) As per (i), what is the probability that the cards have different color? 3
- (d) As per (ii), what is the probability that the cards are aces of same color? 4

8. **The probability distribution of a discrete random variable X is given below:**

x	-2	-1	0	1	3	4
P(x)	0.1	k	2k	3k	4k	0.2

- (a) What is $\sum P(x)$? 1
- (b) Find the value of k. 2
- (c) Find $P(X \geq 0)$ & $P(X < 1)$ 3
- (d) Find the cumulative distribution function, F(X) and F(2) and explain. 4